

Algebraic Number Theory

(PARI-GP version 2.11.0)

Binary Quadratic Forms

create $ax^2 + bxy + cy^2$ (distance d)	<code>Qfb(a, b, c, {d})</code>
reduce x ($s = \sqrt{D}$, $l = \lfloor s \rfloor$)	<code>qfbred(x, {flag}, {D}, {l}, {s})</code>
return $[y, g]$, $g \in \text{SL}_2(\mathbf{Z})$, $y = g \cdot x$ reduced	<code>qfbreds12(x)</code>
composition of forms	<code>x*y or qfbnucomp(x, y, l)</code>
n -th power of form	<code>x^n or qfbnupow(x, n)</code>
composition without reduction	<code>qfbcompraw(x, y)</code>
n -th power without reduction	<code>qfbpowraw(x, n)</code>
prime form of disc. x above prime p	<code>qfbprimeform(x, p)</code>
class number of disc. x	<code>qfbclassno(x)</code>
Hurwitz class number of disc. x	<code>qfhclassno(x)</code>
solve $Q(x, y) = p$ in integers, p prime	<code>qfsolve(Q, p)</code>

Quadratic Fields

quadratic number $\omega = \sqrt{x}$ or $(1 + \sqrt{x})/2$	<code>quadgen(x)</code>
minimal polynomial of ω	<code>quadpoly(x)</code>
discriminant of $\mathbf{Q}(\sqrt{x})$	<code>quaddisc(x)</code>
regulator of real quadratic field	<code>quadregulator(x)</code>
fundamental unit in real $\mathbf{Q}(\sqrt{D})$	<code>quadunit(D, f'w)</code>
class group of $\mathbf{Q}(\sqrt{D})$	<code>quadclassunit(D, {flag}, {t})</code>
Hilbert class field of $\mathbf{Q}(\sqrt{D})$	<code>quadhilbert(D, {flag})</code>
... using specific class invariant ($D < 0$)	<code>polclass(D, {inv})</code>
ray class field modulo f of $\mathbf{Q}(\sqrt{D})$	<code>quadray(D, f, {flag})</code>

General Number Fields: Initializations

The number field $K = \mathbf{Q}[X]/(f)$ is given by irreducible $f \in \mathbf{Q}[X]$. We denote $\theta = \bar{X}$ the canonical root of f in K . A nf structure contains a maximal order and allows operations on elements and ideals. A bnf adds class group and units. A bnr is attached to ray class groups and class field theory. A rnf is attached to relative extensions L/K .

init number field structure nf

known integer basis B

order maximal at $vp = [p_1, \dots, p_k]$

order maximal at all $p \leq P$

certify maximal order

nf members:

a monic $F \in \mathbf{Z}[X]$ defining K

number of real/complex places

discriminant of nf

T_2 matrix

complex roots of F

integral basis of \mathbf{Z}_K as powers of θ

different/codifferent

index $[\mathbf{Z}_K : \mathbf{Z}[X]/(F)]$

recompute nf using current precision

init relative $rnf L = K[Y]/(g)$

init bnf structure

bnf members:

same as nf , plus

underlying nf

classgroup

regulator

fundamental/torsion units

compress a bnf for storage

recover a bnf from compressed $bnfz$

add S -class group and units, yield $bnfS$

init class field structure bnr

bnr members: same as bnf , plus

underlying bnf

big ideal structure

modulus

structure of $(\mathbf{Z}_K/m)^*$

Fields, subfields, embeddings

Defining polynomials, embeddings

smallest poly defining $f = 0$ (slow)

small poly defining $f = 0$ (fast)

random Tschirnhausen transform of f

$\mathbf{Q}[t]/(f) \subset \mathbf{Q}[t]/(g)$? Isomorphic?

reverse polmod $a = A(t) \bmod T(t)$

compositum of $\mathbf{Q}[t]/(f)$, $\mathbf{Q}[t]/(g)$

compositum of $K[t]/(f)$, $K[t]/(g)$

splitting field of K (degree divides d)

signs of real embeddings of x

complex embeddings of x

$T \in K[t]$, # of real roots of $\sigma(T) \in R[t]$

Subfields, polynomial factorization

subfields (of degree d) of nf

d -th degree subfield of $\mathbf{Q}(\zeta_n)$

roots of unity in nf

roots of g belonging to nf

factor g in nf

factor g mod prime pr in nf

Linear and algebraic relations

poly of degree $\leq k$ with root $x \in \mathbf{C}$

alg. dep. with pol. coeffs for series s

small linear rel. on coords of vector x

Basic Number Field Arithmetic (nf)

Number field elements are `t_INT`, `t_FRAC`, `t_POL`, `t_POLMOD`, or `t_COL` (on integral basis `nf.zk`).

Basic operations

$x + y$

$x \times y$

x^n , $n \in \mathbf{Z}$

x/y

$q = x \setminus y := \text{round}(x/y)$

$r = x \% y := x - (x \setminus y)y$

... $[q, r]$ as above

reduce x modulo ideal A

absolute trace $\text{Tr}_{K/\mathbf{Q}}(x)$

absolute norm $N_{K/\mathbf{Q}}(x)$

Multiplicative structure of K^* ; $K^*/(K^*)^n$

valuation $v_p(x)$

... write $x = \pi^{v_p(x)} y$

quadratic Hilbert symbol (at \mathfrak{p})

b such that $xb^n = v$ is small

`bnfcompress(bnf)`

`bnfinit(bnfz)`

`bnfsunit(bnf, S)`

`bnrinit(bnf, m, {flag})`

`bnr.bn`

`bnr.bid`

`bnr.mod`

`bnr.zkst`

`polredabs(f, {flag})`

`polredbest(f, {flag})`

`poltschirnhaus(f)`

`nfisincl(f, g), nfisom`

`modreverse(a)`

`polcompositum(f, g, {flag})`

`nfcompositum(nf, f, g, {flag})`

`nfsplitting(nf, {d})`

`nfeltsign(nf, x, {pl})`

`nfeltembed(nf, x, {pl})`

`nfpolsturm(nf, T, {pl})`

`nfsubfields(nf, {d})`

`polsubcyclo(n, d, {v})`

`nfrootssof1(nf)`

`nfroots(nf, g)`

`nfactor(nf, g)`

`nffactormod(nf, g, pr)`

`algdep(x, k)`

`seralgdep(s, x, y)`

`lindep(x)`

`nfeltadd(nf, x, y)`

`nfeltmul(nf, x, y)`

`nfeltpow(nf, x, n)`

`nfeltdiv(nf, x, y)`

`nfeltdiveuc(nf, x, y)`

`nfeltdmod(nf, x, y)`

`nfeltdivrem(nf, x, y)`

`nfeltreduce(nf, x, A)`

`nfelttrace(nf, x)`

`nfeltnorm(nf, x)`

`nfeltval(nf, x, p)`

`nfeltval(nf, x, p, &y)`

`nfhilbert(nf, a, b, {p})`

`idealredmodpower(nf, x, n)`

Maximal order and discriminant

integral basis of field $\mathbf{Q}[x]/(f)$

field discriminant of field $f = 0$

express x on integer basis

express element x as a polmod

`nfbasis(f)`

`nfdisc(f)`

`nfalglobasis(nf, x)`

`nfbasistoalg(nf, x)`

Dedekind Zeta Function ζ_K , Hecke L series

$R = [c, w, h]$ in initialization means we restrict $s \in \mathbf{C}$ to domain $|\Re(s) - c| < w$, $|\Im(s)| < h$; $R = [w, h]$ encodes $[1/2, w, h]$ and $[h]$ encodes $R = [1/2, 0, h]$ (critical line up to height h).

ζ_K as Dirichlet series, $N(I) < b$

`dirzetak(nf, b)`

init $\zeta_K^{(k)}$ for $k \leq n$

`lfun(L, s, {n = 0})`

compute $\zeta_K(s)$ (n -th derivative)

`lfunlambda(L, s, {n = 0})`

init $L_K^{(k)}$ for $k \leq n$

`lfuninit([bnr, chi], R, {n = 0})`

compute $L_K(s)$ (n -th derivative)

`lfun(L, s, {n})`

Artin root number of K

`bnrrootnumber(bnr, chi, {flag})`

$L(1, \chi)$, for all χ trivial on H

`bnrL1(bnr, {H}, {flag})`

Class Groups & Units (bnf, bnr)

Class field theory data $a_1, \{a_2\}$ is usually bnr (ray class field), bnr, H (congruence subgroup) or bnr, χ (character on $bnr.clgp$). Any of these define a unique abelian extension of K .

remove GRH assumption from bnf

`bnfcertify(bnf)`

expo. of ideal x on class gp

`bnfisprincipal(bnf, x, {flag})`

expo. of ideal x on ray class gp

`bnrisprincipal(bnr, x, {flag})`

expo. of x on fund. units

`bnfisunit(bnf, x)`

as above for S -units

`bnfissunit(bnfs, x)`

signs of real embeddings of $bnf.fu$

`bnfsignunit(bnf)`

narrow class group

`bnfnarrow(bnf)`

Class Field Theory

ray class number for modulus m

`bnrclassno(bnf, m)`

discriminant of class field

`bnrdisc(a1, {a2})`

ray class numbers, l list of moduli

`bnrclassnolist(bnf, l)`

discriminants of class fields

`bnrdisclist(bnf, l, {arch}, {flag})`

decode output from $bnrdisclist$

`bnfdecodemodule(nf, fa)`

is modulus the conductor?

`bnrisconductor(a1, {a2})`

is class field (bnr, H) Galois over K^G

`bnrisgalois(bnr, G, H)`

action of automorphism on $bnr.gen$

`bnrgaloismatrix(bnr, aut)`

apply $bnrgaloismatrix$ M to H

`bnrgaloisapply(bnr, M, H)`

characters on $bnr.clgp$ s.t. $\chi(g_i) = e(v_i)$

`bnrchar(bnr, g, {v})`

conductor of character χ

`bnrconductor(bnr, chi)`

conductor of extension

`rnfconductor(bnf, g)`

Artin group of extension $K[Y]/(g)$

`rnfnormgroup(bnr, g)`

subgroups of bnr , index $\leq b$

`subgrouplist(bnr, b, {flag})`

rel. eq. for class field def'd by sub

`rnfkummer(bnr, sub, {d})`

same, using Stark units (real field)

`bnrstark(bnr, sub, {flag})`

is a an n -th power in K_v ?

`nfislocalpower(nf, v, a, n)`

cyclic L/K satisf. local conditions

Ideals: elements, primes, or matrix of generators in HNF

is *id* an ideal in *nf*?

is *x* principal in *bnf*?

give $[a, b]$, s.t. $a\mathbf{Z}_K + b\mathbf{Z}_K = x$

put ideal $a(a\mathbf{Z}_K + b\mathbf{Z}_K)$ in HNF form

norm of ideal *x*

minimum of ideal *x* (direction *v*)

LLL-reduce the ideal *x* (direction *v*)

Ideal Operations

add ideals *x* and *y*

multiply ideals *x* and *y*

intersection of ideals *x* and *y*

n-th power of ideal *x*

inverse of ideal *x*

divide ideal *x* by *y*

Find $(a, b) \in x \times y$, $a + b = 1$

coprime integral *A, B* such that $x = A/B$

```
nfisideal(nf, id)
bnfisprincipal(bnf, x)
idealtwoel(nf, x, {a})
idealhnf(nf, x, {b})
idealnorm(nf, x)
idealmin(nf, x, v)
idealred(nf, x, {v})
```

```
idealadd(nf, x, y)
idealmul(nf, x, y, {flag})
idealintersect(nf, x, y, {flag})
idealpow(nf, x, n, {flag})
idealinv(nf, x)
idealdiv(nf, x, y, {flag})
idealaddtoone(nf, x, {y})
idealnumden(nf, x)
```

Primes and Multiplicative Structure

factor ideal *x* in \mathbf{Z}_K

expand ideal factorization in *K*

is ideal *A* an *n*-th power?

expand elt factorization in *K*

decomposition of prime *p* in \mathbf{Z}_K

valuation of *x* at prime ideal *pr*

weak approximation theorem in *nf*

a $\in K$, s.t. $v_p(a) = v_p(x)$ if $v_p(x) \neq 0$

a $\in K$ such that $(a \cdot x, y) = 1$

give *bid* =structure of $(\mathbf{Z}_K/\text{id})^*$

structure of $(1 + \mathfrak{p})/(1 + \mathfrak{p}^k)$

discrete log of *x* in $(\mathbf{Z}_K/\text{bid})^*$

idealstar of all ideals of norm $\leq b$

add Archimedean places

init modpr structure

project *t* to \mathbf{Z}_K/pr

lift from \mathbf{Z}_K/pr

Galois theory over \mathbf{Q}

conjugates of a root θ of *nf*

apply Galois automorphism *s* to *x*

Galois group of field $\mathbf{Q}[x]/(f)$

initializes a Galois group structure *G*

character table of *G*

conjugacy classes of *G*

$\det(1 - \rho(g)T)$, χ character of ρ

$\det(\rho(g))$, χ character of ρ

action of *p* in nfgaloisconj form

identify as abstract group

export a group for GAP/MAGMA

subgroups of the Galois group *G*

is subgroup *H* normal?

subfields from subgroups

fixed field

Frobenius at maximal ideal *P*

ramification groups at *P*

is G abelian?

abelian number fields/ \mathbf{Q}

```
idealfactor(nf, x)
idealfactorback(nf, f, {e})
idealispower(nf, A, n)
nffactorback(nf, f, {e})
idealprimedec(nf, p)
ideaval(nf, x, pr)
idealchinese(nf, x, y)
idealappr(nf, x)
idealcoprime(nf, x, y)
idealstar(nf, id, {flag})
idealprincipalunits(nf, pr, k)
ideallog(nf, x, bid)
ideallist(nf, b, {flag})
ideallistarch(nf, b, {ar}, {flag})
nfmodprin(nf, pr)
nfmodpr(nf, t, modpr)
nfmodprlift(nf, t, modpr)
```

```
nfgaloisconj(nf, {flag})
nfgaloisapply(nf, s, x)
polgalois(f)
galoisinit(pol, {den})
galoischartable(G)
galoisconjclasses(G)
galoischarpoly(G, x, {o})
galoischardet(G, x, {o})
galoispermtopol(G, {p})
galoisidentify(G)
galoisexport(G, {flag})
galoissubgroups(G)
galoisnormal(G, H)
galoisbasis(G, H)
galoissubfields(G, {flag}, {v})
galoisfixedfield(G, perm, {flag}, {v})
idealfrobenius(nf, G, P)
idealramgroups(nf, G, P)
galoisisabelian(G, {flag})
galoissubcyclo(N, H, {flag}, {v})
```

Algebraic Number Theory

(PARI-GP version 2.11.0)

The galpol package

query the package: polynomial
... : permutation group
... : group description

Relative Number Fields (rnf)

Extension L/K is defined by $T \in K[x]$.

absolute equation of *L*

is L/K abelian?

relative nfalgobasis

relative nfbasioal

relative idealhnf

relative idealmul

relative idealtwoelt

Lifts and Push-downs

absolute \rightarrow relative representation for *x*

relative \rightarrow absolute representation for *x*

lift *x* to the relative field

push *x* down to the base field

idem for *x* ideal: (rnfideal)reltoabs, abstorel, up, down

Norms and Trace

relative norm of element $x \in L$

relative trace of element $x \in L$

absolute norm of ideal *x*

relative norm of ideal *x*

solutions of $N_K/\mathbf{Q}(y) = x \in \mathbf{Z}$

is $x \in \mathbf{Q}$ a norm from *K*?

initialize *T* for norm eq. solver

is $a \in K$ a norm from *L*?

initialize *t* for Thue equation solver

solve Thue equation $f(x, y) = a$

characteristic poly. of *a* mod *T*

Factorization

factor ideal *x* in *L*

$[S, T]: T_{i,j} \mid S_i$; *S* primes of *K* above *p* rnfidealprimedec(rnf, p)

Maximal order \mathbf{Z}_L as a \mathbf{Z}_K -module

relative polredbest

relative polredabs

relative Dedekind criterion, prime *pr*

discriminant of relative extension

pseudo-basis of \mathbf{Z}_L

General \mathbf{Z}_K -modules: $M = [\text{matrix, vec. of ideals}] \subset L$

relative HNF / SNF

multiple of $\det M$

HNF of *M* where $d = \text{nf} \det(M)$

reduced basis for *M*

determinant of pseudo-matrix *M*

Steinitz class of *M*

\mathbf{Z}_K -basis of *M* if \mathbf{Z}_K -free, or 0

n-basis of *M*, or $(n+1)$ -generating set

is *M* a free \mathbf{Z}_K -module?

```
galoisgetpol(a,b,{s})
galoisgetgroup(a,b)
galoisgetname(a,b)
```

```
rnfequation(nf, T, {flag})
rnfisabelian(nf, T)
rnfalgobasis(rnf, x)
rnfbasistoalg(rnf, x)
rnfideahnf(rnf, x)
rnfidealhnf(rnf, x)
rnfidealmul(rnf, x, y)
rnfidealtwoelt(rnf, x)
```

```
rnfeltabstore(rnf, x)
rnfeltrelobs(rnf, x)
rnfeltup(rnf, x)
rnfeltdown(rnf, x)
rnfeltnorm(rnf, x)
rnfelttrace(rnf, x)
rnfidealnormabs(rnf, x)
rnfidealnormrel(rnf, x)
bnfisintnorm(bnf, x)
bnfisnorm(bnf, x, {flag})
rnfisnorminit(K, pol, {flag})
rnfisnorm(T, a, {flag})
thueinit(f)
thue(t, a, {sol})
rnfcharpoly(nf, T, a, {v})
```

rnfidealfactor(rnf, x)

rnfidealprimedec(rnf, p)

rnfpolredbest(nf, T)

rnfpolredabs(nf, T)

rnfdedekind(nf, T, pr)

rnfdisc(nf, T)

rnfpsseudobasis(nf, T)

nfhnf(nf, M), nfsnf

nfdetint(nf, M)

nfhnfmod(x, d)

rnfllgram(nf, T, M)

rnfdet(nf, M)

rnfsteinitz(nf, M)

rnfhnfbasis(bnf, M)

rnfbasis(bnf, M)

rnfisfree(bnf, M)

Associative Algebras

A is a general associative algebra given by a multiplication table *mt* (over \mathbf{Q} or \mathbf{F}_p); represented by *al* from algtableinit.
create *al* from *mt* (over \mathbf{F}_p) algtableinit(mt, {p = 0})
group algebra $\mathbf{Q}[G]$ (or $\mathbf{F}_p[G]$) alggroup(G, {p = 0})
center of group algebra alggroupcenter(G, {p = 0})

Properties

is (mt, p) OK for algtableinit? algisassociative(mt, {p = 0})
multiplication table *mt* algmultable(al)
dimension of *A* over prime subfield algdim(al)
characteristic of *A* algchar(al)
is *A* commutative? algiscommutative(al)
is *A* simple? algissimple(al)
is *A* semi-simple? algissemisimple(al)
center of *A* algcenter(al)
Jacobson radical of *A* algradical(al)
radical *J* and simple factors of *A/J* algsimpledec(al)

Operations on algebras

create A/I , I two-sided ideal algquotient(al, I)
create $A_1 \otimes A_2$ algtensor(al1, al2)
create subalgebra from basis *B* algsubalg(al, B)
quotients by ortho. central idempotents *e* algcentralproj(al, e)
isomorphic alg. with integral mult. table algmakeintegral(mt)
prime subalgebra of semi-simple *A* over \mathbf{F}_p algprimesubalg(al)
find isomorphism $A \cong M_d(\mathbf{F}_q)$ algsplit(al)

Operations on lattices in algebras

lattice generated by cols. of *M* alglathnf(al, M)
... by the products xy , $x \in \text{lat1}$, $y \in \text{lat2}$ alglatmul(al, lat1, lat2)
sum $\text{lat1} + \text{lat2}$ of the lattices alglatadd(al, lat1, lat2)
intersection $\text{lat1} \cap \text{lat2}$ alglatinter(al, lat1, lat2)
test $\text{lat1} \subset \text{lat2}$ alglatsubset(al, lat1, lat2)
generalized index $(\text{lat2} : \text{lat1})$ alglatindex(al, lat1, lat2)
 $\{x \in \text{al} \mid x \cdot \text{lat1} \subset \text{lat2}\}$ alglatlefttransporter(al, lat1, lat2)
 $\{x \in \text{al} \mid \text{lat1} \cdot x \subset \text{lat2}\}$ alglatrighttransporter(al, lat1, lat2)
test *x* in *lat* (set *c* = coord. of *x*) alglatcontains(al, lat, x, {&c})
element of *lat* with coordinates *c* alglatelement(al, lat, c)

Operations on elements

$a + b$, $a - b$, $-a$ algadd(al, a, b), algsub(al, a, b), algneg
 $a \times b$, a^2 algmul(al, a, b), algsqr
 a^n , a^{-1} algpow(al, a, n), alginv
is *x* invertible? (then set *z* = x^{-1}) algisinv(al, x, {&z})
find *z* such that $x \times z = y$ algdivl(al, x, y)
find *z* such that $z \times x = y$ algdivr(al, x, y)
does *z* s.t. $x \times z = y$ exist? (set it) algisdivl(al, x, y, {&z})
matrix of $v \mapsto x \cdot v$ algomatrices(al, x)
absolute norm algnorm(al, x)
absolute trace algtrace(al, x)
absolute char. polynomial algcharpoly(al, x)
given *a* $\in A$ and polynomial *T*, return *T(a)* algpoleval(al, T, a)
random element in a box algrandom(al, b)

Based on an earlier version by Joseph H. Silverman

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Send comments and corrections to <Karim.Belabas@math.u-bordeaux.fr>

Central Simple Algebras

A is a central simple algebra over a number field *K*; represented by *al* from **alginit**; *K* is given by a *nf* structure.
create CSA from data **alginit**(*B, C, {v}, {maxord = 1}*)
multiplication table over *K* *B* = *K*, *C* = *mt*
cyclic algebra (*L/K, σ, b*) *B* = *rnf*, *C* = [*sigma, b*]
quaternion algebra (*a, b*)_{*K*} *B* = *K*, *C* = [*a, b*]
matrix algebra *M_d(K)* *B* = *K*, *C* = *d*
local Hasse invariants over *K* *B* = *K*, *C* = [*d, [PR, HF], HI*]

Properties

type of <i>al</i> (<i>mt</i> , CSA)	algtype (<i>al</i>)
dimension of <i>A</i> over Q	algdim (<i>al</i> , 1)
dimension of <i>al</i> over its center <i>K</i>	algdim (<i>al</i>)
degree of <i>A</i> (= $\sqrt{\dim_K A}$)	algdegree (<i>al</i>)
<i>al</i> a cyclic algebra (<i>L/K, σ, b</i>); return <i>σ</i>	algaut (<i>al</i>)
... return <i>b</i>	algb (<i>al</i>)
... return <i>L/K</i> , as an <i>rnf</i>	algsplittingfield (<i>al</i>)
split <i>A</i> over an extension of <i>K</i>	algsplittingdata (<i>al</i>)
splitting field of <i>A</i> as an <i>rnf</i> over center	algsplittingfield (<i>al</i>)
multiplication table over center	algrelmutable (<i>al</i>)
places of <i>K</i> at which <i>A</i> ramifies	algramifiedplaces (<i>al</i>)
Hasse invariants at finite places of <i>K</i>	alghassef (<i>al</i>)
Hasse invariants at infinite places of <i>K</i>	alghassei (<i>al</i>)
Hasse invariant at place <i>v</i>	alghasse (<i>al, v</i>)
index of <i>A</i> over <i>K</i> (at place <i>v</i>)	algindex (<i>al, {v}</i>)
is <i>al</i> a division algebra? (at place <i>v</i>)	algisdivision (<i>al, {v}</i>)
is <i>A</i> ramified? (at place <i>v</i>)	algisramified (<i>al, {v}</i>)
is <i>A</i> split? (at place <i>v</i>)	algissplit (<i>al, {v}</i>)

Operations on elements

reduced norm	algnorm (<i>al, x</i>)
reduced trace	algtrace (<i>al, x</i>)
reduced char. polynomial	algcharpoly (<i>al, x</i>)
express <i>x</i> on integral basis	algalgtobasis (<i>al, x</i>)
convert <i>x</i> to algebraic form	algbasisstoalg (<i>al, x</i>)
map <i>x</i> ∈ <i>A</i> to <i>M_d(L)</i> , <i>L</i> split. field	algtomatrix (<i>al, x</i>)

Orders

Z -basis of order \mathcal{O}_0	algbasis (<i>al</i>)
discriminant of order \mathcal{O}_0	algdisc (<i>al</i>)
Z -basis of natural order in terms \mathcal{O}_0 's basis	alginvbasis (<i>al</i>)

Based on an earlier version by Joseph H. Silverman

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